## Difficulty:

## Box - Hard Puzzle \#40



This puzzle is like a crossword, but with numbers. Each digit occupies a 3D block and can be a part of a "word" in the $\mathrm{X}, \mathrm{Y}$, and Z directions.

## Rules:

1. "Words" may not start with a zero.
2. "Words" in the $X$ direction read from left to right.
3. "Words" in the Y direction read from top to bottom.
4. "Words" in the $Z$ direction read from front to back.
5. There is one unique solution which satisfies all the clues given below.
6. Some "words" may not have clues. They will be determined by the "words" which intersect them.

If we take the box pictured above and divide it into individual $X-Y$ layers, we will get these planes:

| 1 | 2 | 3 | 4 | 18 | 19 | 20 |  | 28 | 29 |  | 30 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 |  | 6 |  | 21 | 22 |  |  | 31 |  | 32 | 33 |
| 7 | 8 |  | 9 | 23 |  |  | 24 | 34 |  | 35 |  |
| 10 | 11 | 12 | 13 | 25 |  | 26 |  | 36 |  |  | 37 |
| 14 | 15 | 16 | 17 | 27 |  |  |  |  | 38 |  |  |
|  |  | 39 |  | 40 | 41 |  | 48 | 49 | 50 |  |  |
|  |  |  |  | 42 |  |  |  | 51 |  |  |  |
|  |  | 43 | 44 |  | 45 | 52 | 53 |  |  |  |  |
|  |  |  | 46 |  |  | 54 |  |  |  |  |  |
|  |  | 47 |  |  |  | 55 |  |  |  |  |  |

## X Direction

1 Y41 plus Z17
6 Z9 minus X51
7 Its digits total X6
10 Seven times a prime number
14 Mean of Y28 and Y26
18 A prime number
21 Y24 plus X47
23 X28 minus Y26
25 Last two digits are the same as last two digits of X34
27 Fifty-four times a prime number
28 Twice X51
31 X43 minus Z33
34 Z8 minus Z16
36 Rearranged digits of Y50
38 A prime number
39 Mean of X18 and Y37
42 Z 33 divided by forty-seven
43 Fifty-seven times a prime number
46 Rearranged digits of X34
47 Y24 minus X28
48 Mean of X52 and X28
51 Mean of Y20 and Y26
52 Y53 plus Y8
54 Two thousand twenty-six more than X1
55 Twice a prime number

## Y Direction

1 Y40 plus X48
3 Nine times a prime number
4 Z22 plus Y29
8 A square
18 Four thousand eight hundred seventy-four less than Y49
19 Twice a prime number
20 Y24 minus Y39
24 A cube
26 Y39 minus X47
28 Four times a prime number
$29 \mathrm{Z7}$ plus half of Y39
30 X38 minus half of X47
32 A prime number
37 Z10 minus Z35
39 A square
40 Nine thousand one more than Y4
41 Fifteen times a prime number
44 Z13 divided by X28
49 First two digits are the same as first two digits of X54
50 Fourteen times a prime number
52 Nine times X6
53 Thirteen times a prime number

## Z Direction

1 Mean of X1 and Y28
2 Last two digits are the same as last two digits of Z15
3 X6 plus Z45
4 Forty-eight times a prime number
5 Twenty-six times a prime number
6 Six thousand four hundred two less than Z12
7 Thirty-one times a prime number
8 A prime number
9 Mean of X28 and Z14
10 Twice the result of Z35 minus Z9
11 Seven thousand eight hundred sixty-six more than Z4
12 Mean of Z11 and Y52
13 One thousand eight hundred ninety more than X54
14 Y44 divided by three
15 Mean of Z6 and Z14
16 Fifty-six times a prime number
17 Rearranged digits of Y24
22 Sum of digits in Y18
33 X36 minus X52
35 Y24 minus X34
40 Y30 minus X42
45 X43 minus half of Y50
47 Z40 minus Y37

## Solution:

| 7 | 4 | 3 | 6 | 8 | 5 | 2 | 1 | 8 | 6 |  | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 |  | 2 | 2 | 9 | 3 | 8 |  | 3 | 2 | 6 | 8 |
| 6 | 9 | 1 | 6 | 2 | 8 |  | 5 | 3 | 5 | 1 |  |
| 1 | 6 | 3 | 1 | 9 | 9 | 5 | 1 | 2 | 8 | 0 | 3 |
| 4 | 1 | 9 | 5 | 4 | 4 | 8 | 2 |  | 3 | 1 | 1 |
|  |  | 4 | 2 | 7 | 6 |  | 9 | 9 | 8 |  |  |
|  | 8 |  | 1 | 9 |  |  | 4 | 3 |  |  |  |
|  | 4 | 1 | 6 | 1 | 1 | 9 | 1 | 0 |  |  |  |

