## Difficulty:

## Cube - Hard Puzzle \#21



This puzzle is like a crossword, but with numbers. Each digit occupies a 3D block and can be a part of a "word" in the $\mathrm{X}, \mathrm{Y}$, and Z directions.

## Rules:

1. "Words" may not start with a zero.
2. "Words" in the $X$ direction read from left to right.
3. "Words" in the Y direction read from top to bottom.
4. "Words" in the Z direction read from front to back.
5. There is one unique solution which satisfies all the clues given below.
6. Some "words" may not have clues. They will be determined by the "words" which intersect them.

If we take the cube pictured above and divide it into individual X - Y layers, we will get these planes:


## X Direction

1 A prime number
5 Z8 divided by X29
8 Thirty times a prime number
12 Twice a prime number
16 Z 4 minus half of X32
19 Sum of digits in X36
21 Same as Z48
23 Mean of Z9 and Y46
26 Eleven times a prime number
27 Mean of X1 and Z3
28 Z1 divided by X39
29 X28 plus Y46
30 A prime number
32 Z49 reversed
34 Y53 plus Y4
36 Nine times a prime number
38 Twice the result of Z5 minus Y3
39 Z3 divided by X19
42 X34 divided by twenty-four
45 X5 minus Z49
47 Z13 times X58
50 One thousand five hundred fifty-six more than X55
55 Y50 minus X29
56 First two digits are the same as first two digits of Z10
57 Mean of Z7 and X27
58 Y8 minus X19

## Y Direction

2 X50 minus X1
3 Four times a prime number
4 X28 plus X5
8 X32 plus Z18
9 Three times a prime number
19 A palindrome
20 Fifty-one times a prime number
21 Nineteen times a prime number
22 Y35 minus Z10
25 Mean of Y33 and X58
30 A prime number
31 Three times a prime number
32 Forty-three times a square
33 Three times a prime number
35 Three times a prime number
40 X56 minus X26
41 Y22 reversed
43 X5 minus Z49
44 A square
46 Z18 minus X28
50 X55 plus Z18
51 Fourteen times a prime number
52 Four thousand eight hundred forty-six less than Y31
53 Eighty-two times a prime number
54 One thousand three hundred eighty-eight less than Y32

## Z Direction

1 X28 times Z41
3 Z11 plus Y43
4 X21 plus X19
5 One thousand eight hundred forty-three less than Y53
6 Twice a prime number
7 Y54 minus Y8
8 X5 times Z18
9 A palindrome
10 Twice the result of Y8 minus Y41
11 Z3 minus X45
12 Four times a prime number
13 Fourteen times a prime number
14 X26 minus Y51
15 Five times a prime number
16 Thirty-one times a prime number
17 First two digits are the same as X21
18 Same as X29
19 Eleven times a prime number
23 Seventy-three times Y46
24 One thousand three hundred
eighty-six more than X27
29 Its digits total Y44
37 Five times a prime number
41 Same as X30
48 Mean of Y22 and X5
49 Mean of Y43 and X32

## Solution:

|  | 7 | 5 | 9 |  | 1 | 2 | 2 | 7 |  |  | 9 |  | 1 | 3 |  | 7 | 9 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 6 |  | 9 | 4 | 4 | 5 |  | 4 | 3 |  | 3 | 1 | 6 |  | 4 | 4 |
| 1 | 9 | 2 | 9 |  | 0 | 3 | 3 | 0 |  | 9 | 1 |  |  | 1 |  |  | 9 | 9 |
| 7 | 3 | 8 | 2 |  |  | 4 | 4 | 2 |  | 9 | 5 |  |  | 9 |  |  | 8 |  |
| 6 | 9 |  |  |  |  |  | 2 | 1 |  |  | 7 |  | 8 | 3 |  | 7 | 7 |  |
|  |  |  | 2 |  |  | 3 |  |  |  | 1 | 1 | 2 | 7 | 1 | 1 | 9 |  |  |
|  |  |  | 6 | 8 |  | 1 |  |  | 2 | 1 | 1 | 1 | 1 | 6 | 6 | 3 |  |  |
|  |  |  | 8 | 0 |  |  |  |  | 5 |  | 2 | 9 | 9 | 1 | 1 | 5 |  |  |
|  |  |  | 2 |  |  |  | 5 |  |  | 4 | 4 | 8 | 8 | 5 | 5 | 9 |  |  |
|  |  |  | 4 | 7 |  | 9 | 7 |  | 8 |  | 1 |  | 1 | 4 | 4 | 9 |  |  |

