## Cube - Hard Puzzle \#40



This puzzle is like a crossword, but with numbers. Each digit occupies a 3D block and can be a part of a "word" in the $\mathrm{X}, \mathrm{Y}$, and Z directions.

## Rules:

1. "Words" may not start with a zero.
2. "Words" in the $X$ direction read from left to right.
3. "Words" in the Y direction read from top to bottom.
4. "Words" in the Z direction read from front to back.
5. There is one unique solution which satisfies all the clues given below.
6. Some "words" may not have clues. They will be determined by the "words" which intersect them.

If we take the cube pictured above and divide it into individual $X-Y$ layers, we will get these planes:


## X Direction

2 Mean of X32 and Z8
5 Z35 minus Z5
9 Eleven thousand two hundred eighty more than Y35
14 X45 minus half of Y1
17 Z15 minus X59
21 Fourteen times a prime number
25 Eight thousand one hundred seventy-seven less than X9
28 Y2 minus Z17
29 Eighteen times a prime number
31 Z8 plus X2
32 Consecutive digits unordered
36 First two digits are the same as first two digits of X54
38 Twice a prime number
39 Z16 minus Y33
40 Mean of Z5 and Y56
41 Seventy-four times a prime number
45 Twenty-four less than Z5
46 Ninety-six times a prime number
48 Rearranged digits of Y47
49 Thirty-one times Y47
51 Z49 plus Y56
54 Mean of Z50 and Z22
57 Fifty-two times a prime number
58 Same as X51
59 A prime number

## Y Direction

1 X5 minus X58
2 Eight times a prime number
4 Nine thousand nine hundred five less than Y34
6 Four hundred eighty-six less than Y43
21 Y37 times Z8
22 Twice X49
23 Twenty-one times a prime number
24 Sixteen times a prime number
27 Eighteen times a prime number
32 Z8 minus Y1
33 Three times a prime number
34 Forty-nine times a prime number
35 Five times a prime number
37 X49 divided by seventy-three
42 Fifteen times Z49
43 Twice a prime number
44 Half of Z10, then subtract Y43
46 A palindrome
47 Y22 divided by Y56
52 Y24 plus half of Z13
53 A prime number
55 A prime number
56 X58 minus Z49

## Z Direction

1 Three thousand three hundred twenty-six more than Z12
2 Nine times a prime number
3 Mean of X14 and X40
5 Mean of Y46 and Y56
6 Forty-eight times a prime number
7 Y34 minus half of Z1
8 X57 minus X38
9 Z5 divided by three
10 Fourteen thousand twenty-eight more than Y21
11 Nine thousand less than Y21
12 Three thousand two hundred four more than Y43
13 Thirty-two times a prime number
14 Twenty-eight times Z49
15 Sixty-nine times a prime number
16 Four thousand eight hundred forty-eight more than Z10
17 Mean of X45 and Z9
18 Mean of Y23 and X2
19 Three thousand one hundred fifty-nine less than Z18
20 X49 minus X54
22 Rearranged digits of Y24
26 Twice a prime number
29 Two-thirds of Y42
30 Rearranged digits of Z8
35 X48 minus X14
49 Y32 minus X14
50 Mean of Z3 and X45

## Solution:

| 1 |  | 4 | 7 |  | 7 | 6 | 4 |  | 5 | 4 |  |  | 7 | 6 | 6 | 8 |  | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 9 | 7 |  |  | 1 | 3 | 9 | 9 | 3 | 3 |  | 8 | 2 | 3 | 3 | 1 | 3 | 6 |
| 4 | 7 | 5 | 1 |  | 5 | 4 | 7 | 7 | 4 | 3 |  | 6 |  | 4 | 4 | 4 | 4 | 2 |
|  | 5 | 1 |  |  | 8 | 2 | 8 | 8 | 0 | 6 |  | 2 | 1 | 8 | 8 | 8 | 1 | 3 |
| 7 | 2 | 2 |  |  | 2 | 6 | 6 |  | 3 |  |  | 2 |  |  | 9 | 7 |  | 5 |
|  |  |  | 6 | 3 | 1 |  | 2 | 2 |  | 8 | 3 |  |  |  | 9 |  |  |  |
|  |  |  |  | 1 | 0 |  | 8 |  |  |  | 2 | 3 | 3 | 6 | 2 |  |  |  |
|  |  |  | 2 | 5 | 2 |  | 4 | 8 |  |  | 4 | 6 | 6 | 2 | 8 |  |  |  |
|  |  |  | 0 |  | 3 |  | 8 | 0 |  |  | 8 | 3 | 3 |  | 2 |  |  |  |
|  |  |  | 2 | 4 | 8 |  | १ | 3 |  | 1 | 0 | 1 | 1 | 1 | 1 |  |  |  |

