## Pyramid

This puzzle is a 3D pyramid.

Here is a view from the corner where the front and right faces meet (The floor has labels for the faces):


There is no good way to lay it flat so I created some animations to help understand the layout.

Here is an animation of the blocks from the front:
http://3dmathpuzzles.com/animations/Pyramid/front.gif

Here is an animation of the blocks from the right:
http://3dmathpuzzles.com/animations/Pyramid/right.gif

Here is an animation to help you understand the blocks in the Z direction:
http://3dmathpuzzles.com/animations/Pyramid/z.gif

This puzzle is like a crossword, but with numbers. Each digit occupies a 3D shape and can be a part of a "word" in the $\mathrm{X}, \mathrm{Y}$, and Z directions.

## Rules:

1. "Words" may not start with a zero.
2. "Words" read from:
a. X Direction: Left to right when facing the pyramid from the front. For example: blocks 2, 3, and 4 form a "word" in the X direction.
b. Y Direction: Front to back when facing the pyramid from the front. If you face the pyramid from the right, the digits will read left to right. For example: blocks 8, a non-numbered block, 9, a non-numbered block, and 10 form a "word" in the $Y$ direction.
c. Z Direction: Top to bottom of the pyramid, in a vertical line. You can think of these as vertically aligned diamond shapes.
3. There is one unique solution which satisfies all the given clues.
4. Some "words" may not have clues. They will be determined by the "words" which intersect them.

## Clues

| X | Direction |  |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{2}$ | Y30 plus Z43, then multiply by seven | $\mathbf{4 7}$ | Mean of Z18 and Z19 |
| $\mathbf{5}$ | Y51 divided by the result of X13 minus | $\mathbf{4 9}$ | Sum of X5, Y35, and Z17 |
|  | Y21 |  |  |
| $\mathbf{1 1}$ | Y25 divided by Z38 | $\mathbf{5 0}$ | First, fifth, and sixth digits are the same |
| $\mathbf{1 3}$ | Mean of X5 and X45 | $\mathbf{5 1}$ | X47 plus twice X49 |
| $\mathbf{2 0}$ | Seven times a prime number | $\mathbf{5 4}$ | Nine times the sum of X46, Y21, and Y30 |
| $\mathbf{2 4}$ | X45 times the median of X67 and Y60 | $\mathbf{5 5}$ | Y14 minus Y30, then multiply by a prime number |
| $\mathbf{2 8}$ | Y48 rearranged | $\mathbf{5 7}$ | Eight times the difference of Z64 and Z41 |
| $\mathbf{2 9}$ | Sum of X38, Y8, and Z54, then subtract | $\mathbf{5 8}$ | X54 minus the result of X59 multiplied by ten |
|  | Z38 |  |  |
| $\mathbf{3 1}$ | Y27 times Z41 | $\mathbf{5 9}$ | Add X67 and Y26, then divide by 2 |
| $\mathbf{3 3}$ | Z64 minus Y30 | $\mathbf{6 0}$ | Y4 times Z1 |
| $\mathbf{3 4}$ | Is a prime number | $\mathbf{6 1}$ | A 3 digit prime number multiplied by a 4 digit |
|  |  | prime number |  |
| $\mathbf{3 5}$ | X45 plus a square, then multiply by two | $\mathbf{6 2}$ | Is a prime number |
| $\mathbf{3 6}$ | Y30 plus Z4 | $\mathbf{6 3}$ | X62 minus Y52 |
| $\mathbf{3 8}$ | Z44 minus X67 | $\mathbf{6 4}$ | Twice a prime number |
| $\mathbf{3 9}$ | X58 plus Y57 | $\mathbf{6 5}$ | Is a prime number |
| $\mathbf{4 1}$ | Twice Y30 times Y60 | $\mathbf{6 6}$ | Y35 minus Z17 |
| $\mathbf{4 5}$ | Is a prime number | $\mathbf{6 7}$ | Y20 minus Z5, then divide by the reverse of X11 |
| $\mathbf{4 6}$ | Three times a prime number |  |  |

## Y Direction

2 Same as Y48
3 X49 plus half of X38
4 Same as Z4
5 Second and last digits are the same
6 X41 plus three, then multiply by Z56
7 X20 minus Y53
8 Sum of X58, Y30, and Z38, then subtract X13

11 Four less than X35
12 X34 times Z54
13 X13 times Z2
14 X47 plus Z7

15 Ten times a prime number
16 First and last digits are the same
20 Sum of X2, Y62, and Z11
21 X66 plus Z19
22 Z39 minus the reverse of X11, then multiply by X34

23 X28 plus Z39, then subtract Z19

24 Rearranged digits of Y2 multiplied by Z18
25 X11 times Z38
26 Y22 divided by X34
27 Twice the result of Y8 minus both Y2 and Z56
30 Z1 divided by X34
32 Second and fourth digits are the same
35 X66 plus reversed Z41

37 Z7 plus Z41
42 Twice Z19, then add X41 and Z40
48 Is a square
51 Five times the sum of Y2, three times Y11, and Z18

52 Second digit is same as fourth
53 First and third digits are the same
57 Twice a prime number
60 Y37 reversed
62 Three times a prime number

## Z Direction

1 Consecutive digits in descending order
2 Y13 divided by X13
4 Twice Y3 minus Y21, then divide by Z18
5 X5 minus the sum of Z18 and Z19
7 Z54 minus X13, then divide by four
8 X59 plus the mean of X67 and Y60
9 Four times X47
10 X55 minus Z41, then divide by Y20
11 Twice the difference of Z44 and Y4
14 Sum of Y14, Y35, and Y42, then divide by X47
17 Z41 reversed

18 Y24 divided by X28
19 Y21 minus X66
38 Consecutive digits in order
39 Twice the sum of X57 and Z19
40 Four times X36
$41 \quad$ Y48 minus X2
43 Sum of X67 and Y30
44 X38 plus X67
54 Z56 times a prime
56 X50 divided by Y27

64 Z18 reversed

## Solution starts on next page

## Solution

| X Direction |  |  |  |
| :---: | ---: | ---: | ---: |
| $\mathbf{2}$ | 763 | 47 | 32 |
| $\mathbf{5}$ | 565 | 49 | 652 |
| $\mathbf{1 1}$ | 71 | $\mathbf{5 0}$ | $2,805,228$ |
| $\mathbf{1 3}$ | 289 | $\mathbf{5 1}$ | 1,336 |
| $\mathbf{2 0}$ | 99,113 | $\mathbf{5 4}$ | 49,329 |
| $\mathbf{2 4}$ | 338 | $\mathbf{5 5}$ | 867,683 |
| $\mathbf{2 8}$ | 874 | 57 | 416 |
| $\mathbf{2 9}$ | 45,149 | $\mathbf{5 8}$ | 44,859 |
| $\mathbf{3 1}$ | $2,031,372$ | $\mathbf{5 9}$ | 447 |
| $\mathbf{3 3}$ | 31 | $\mathbf{6 0}$ | $2,980,236$ |
| $\mathbf{3 4}$ | 2,087 | $\mathbf{6 1}$ | 320,797 |
| $\mathbf{3 5}$ | 7,226 | $\mathbf{6 2}$ | 959,873 |
| $\mathbf{3 6}$ | 76 | $\mathbf{6 3}$ | 310,422 |
| $\mathbf{3 8}$ | 44 | $\mathbf{6 4}$ | $7,127,602$ |
| $\mathbf{3 9}$ | 88,621 | $\mathbf{6 5}$ | 743 |
| $\mathbf{4 1}$ | 2,268 | $\mathbf{6 6}$ | 63 |
| $\mathbf{4 5}$ | 13 | $\mathbf{6 7}$ | 25 |
| $\mathbf{4 6}$ | 5,349 |  |  |


| Y Direction |  |  |  |
| :---: | ---: | ---: | ---: |
| $\mathbf{2}$ | 784 | $\mathbf{2 4}$ | 32,338 |
| $\mathbf{3}$ | 674 | $\mathbf{2 5}$ | 324,257 |
| $\mathbf{4}$ | 34 | 26 | 869 |
| $\mathbf{5}$ | 54,864 | $\mathbf{2 7}$ | 96,732 |
| $\mathbf{6}$ | 65,859 | $\mathbf{3 0}$ | 42 |
| $\mathbf{7}$ | 51,623 | $\mathbf{3 2}$ | 360,682 |
| $\mathbf{8}$ | 49,179 | $\mathbf{3 5}$ | 75 |
| $\mathbf{1 1}$ | 7,222 | $\mathbf{3 7}$ | 72 |
| $\mathbf{1 2}$ | $1,028,891$ | 42 | 2,626 |
| $\mathbf{1 3}$ | $2,185,707$ | 48 | 784 |
| $\mathbf{1 4}$ | 83 | $\mathbf{5 1}$ | 112,435 |
| $\mathbf{1 5}$ | $9,732,830$ | $\mathbf{5 2}$ | 649,451 |
| $\mathbf{1 6}$ | 218,362 | 53 | 47,490 |
| $\mathbf{2 0}$ | 926 | $\mathbf{5 7}$ | 43,762 |
| $\mathbf{2 1}$ | 90 | $\mathbf{6 0}$ | 27 |
| $\mathbf{2 2}$ | $1,813,603$ | $\mathbf{6 2}$ | 93 |
| $\mathbf{2 3}$ | 1,733 |  |  |


| Z Direction |  |  |  |
| :---: | ---: | :---: | ---: |
| 1 | 87,654 | 18 | 37 |
| 2 | 7,563 | 19 | 27 |
| 4 | 34 | 38 | 4,567 |
| 5 | 501 | 39 | 886 |
| 7 | 51 | 40 | 304 |
| 8 | 473 | 41 | 21 |
| 9 | 128 | 43 | 67 |
| 10 | 937 | 54 | 69 |
| 11 | 70 | 56 | 493 |
| 14 | 87 | 64 | 29 |
| 17 | 12 |  | 73 |

